ON THE CHROMATOGRAPHY OF RECIPROCAL SALT SYSTEMS*

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Chromatography of a reciprocal salt system composed of monovalent cations C¹ and C², and anions A¹ and A², can produce up to four bands or spots. It is not immediately apparent without a detailed analysis of the problem, however, how many bands will be observed and what will be their relative intensities. Four spots have been reported in paper chromatography¹ and in thin-layer chromatography on silica gel G^2 , the inner spots being less intense than the extreme spots in the latter case.

This report describes the results of application of distribution theory to this and a related system, and comparison of the theoretical predictions with available experimental results.

METHOD

The pertinent equilibrium expressions are

$$C^{1}A^{1} + C^{2}A^{2} \stackrel{K^{M}}{\leq} C^{1}A^{2} + C^{2}A^{1} \quad K^{M} = \frac{(C^{1}A^{2})^{M} (C^{2}A^{1})^{M}}{(C^{1}A^{1})^{M} (C^{2}A^{2})^{M}}$$
(1)

$$(C^{1}A^{1})^{F} = K_{D}^{11} (C^{1}A^{1})^{M}$$
(2)

$$(C^{1}A^{2})^{F} = K_{D}^{12} (C^{1}A^{2})^{M}$$
(3)
$$(C^{2}A^{1})^{F} = K_{D}^{21} (C^{2}A^{1})^{M}$$
(4)

$$(\mathbf{C}^{*}\mathbf{A}^{*})^{*} \equiv \mathbf{A} \mathbf{D}^{**} (\mathbf{C}^{*}\mathbf{A}^{*})^{**}$$
(4)

$$(C^2 A^2)^F = K_D^{22} (C^2 A^2)^M$$
 (5)

 $(C^{1}A^{1})^{F} + (C^{1}A^{1})^{M} + (C^{1}A^{2})^{F} + (C^{1}A^{2})^{M} = T^{11} + T^{12}$ (6)

$$(C^{1}A^{2})^{F} + (C^{1}A^{2})^{M} + (C^{2}A^{2})^{F} + (C^{2}A^{2})^{M} = T^{12} + T^{22}$$
(7)

$$(C^{2}A^{1})^{F} + (C^{2}A^{1})^{M} + (C^{2}A^{2})^{F} + (C^{2}A^{2})^{M} = T^{21} + T^{22}$$
(8)

$$(C^{1}A^{1})^{F} + (C^{1}A^{1})^{M} + (C^{2}A^{1})^{F} + (C^{2}A^{1})^{M} = T^{11} + T^{21}$$
(9)

where $()^{F}$ and $()^{M}$ denote concentrations in the fixed and mobile phases and T^{ij} represents the total concentration of C'A' charged into a given plate before equilibration. Simultaneous solution of (1)-(5) and any three of (6)-(9) affords straightforward though involved analytical expressions for the eight variables $(C^{i}A^{j})^{F}$ and $(C^{i}A^{j})^{M}$.

(2)

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^{*} Contribution No. 1677 from the Woods Hole Oceanographic Institution. Supported in part by the Office of Naval Research, Contract Nonr 2196 (00).

Plate theory computations for this system were carried out using a General Electric 225 computer. The first cells of banks of equal volume cells of the two phases were opposed, one mole each of C^1A^1 and C^2A^2 or C^1A^2 and C^2A^1 was charged into the first cell of the fixed phase, the equilibrium values of $(C^iA^j)^F$ and $(C^iA^j)^M$ were computed, the mobile bank of cells was advanced to the next plate, new T^{ij} and then new (C^iA^j) were computed for each cell and so on until the requisite number of plates had been equilibrated.

This model corresponds to a partition chromatogram in which the rate of attainment of equilibrium is large relative to the rate of flow of the mobile phase. The above formulation of the distribution equilibria assumes that ion pairs are the only important species in both phases.

The computation routine described, when applied to pure, noninteracting components, produced highly symmetrical peaks in 50-plate chromatograms. The reciprocal salt system results obtained invariably satisfied the symmetry and mass balance requirements of the system $(\Sigma(C^{1}A^{1}) = \Sigma(C^{2}A^{2}), \Sigma(C^{1}A^{2}) = \Sigma(C^{2}A^{1}), \Sigma(C^{1}A^{1}) + \Sigma(C^{1}A^{2}) = I$, the summation, here and elsewhere in this paper, extending over all plates of the chromatogram) and the output peak maxima appeared at the R_{F} values required by the values of K_{D}^{ij} read into each run.

RESULTS

The results for 23 runs are given in Table I. Fig. 1 illustrates the course of development of a typical chromatogram. Fortunately, a 200-plate computation (the practical limit in the present work) is sufficient to resolve completely the left and right halves of the chromatogram, though not the individual components of

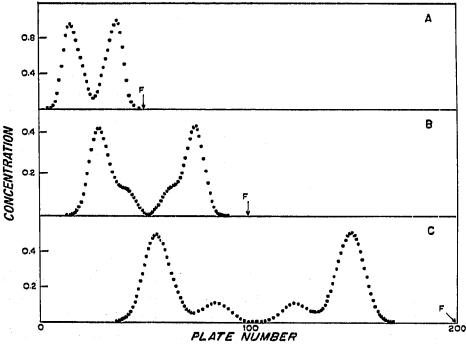


Fig. 1. Partition chromatogram of the system $C^{1}A^{1} + C^{2}A^{2} = C^{1}A^{2} + C^{2}A^{1}$, with $R_{F}^{11} = 0.2727$, $R_{F}^{12} = 0.4286$, $R_{F}^{21} = 0.6000$, $R_{F}^{22} = 0.7500$ and $K^{M} = K^{F} = 1$. After (A) 50; (B) 100; (C) 200 plates (runs 8, 10, 11 of Table I). F marks the solvent front.

TABLE I

CHROMATOGRAMS OF THE SYSTEM C¹A¹-C¹A²-C²A¹-C²A² COMPUTED BY DISTRIBUTION THEORY

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Run	N*	KM	R _F II	R_F^{12}	R_F^{21}	$R_{\rm F}^{22}$	K ¹² K ²¹ K ¹¹ K ²²	$\frac{R_F^{21}-R}{R_F^{22}-R}$	$\frac{R_{\rm F}^{12}}{R_{\rm F}^{11}} \left(X^{12} + X^{21} \right) cor.$	$X^{12} + X^{21}$
j_0 i 0.2730 0.7730 0.7730 1.000 0.402 j_0 i 0.2300 0.3000 0.7300 0.7300 0.402 j_0 i 0.2300 0.3000 0.7300 0.7300 0.307 j_0 i 0.2300 0.3070 0.7300 0.7300 0.307 j_0 i 0.2300 0.7300 0.7300 0.7300 0.371 j_0 i 0.2720 0.3456 0.6000 0.7300 0.3790 0.100 j_0 i 0.2727 0.4286 0.6000 0.7300 0.339 0.1791 j_0 i 0.2727 0.4286 0.6000 0.7300 0.339 0.1776 j_0 i 0.2727 0.4286 0.6000 0.7300 0.100 0.359 0.1872 j_0 i 0.2727 0.4286 0.6000 0.7300 0.1790 0.1795 <td>H H</td> <td>05</td> <td>H</td> <td>0.2500</td> <td>0.2625</td> <td>0.7375</td> <td>0.7500</td> <td>I.000</td> <td>0.950</td> <td>0.4778</td> <td>0.4779</td>	H H	05	H	0.2500	0.2625	0.7375	0.7500	I.000	0.950	0.4778	0.4779
\vec{j} \vec{l}	6	, ç	I	0.2500	0.2750	0.7250	0.7500	I.000	0.000	0.4552	0.4554
\vec{y} I $\alpha_2 g_{00}$ $\alpha_3 g_{00}$ $\alpha_5 g_{00}$ <th< td=""><td>~</td><td>, P</td><td>H</td><td>0.2500</td><td>0.3000</td><td>0.7000</td><td>0.7500</td><td>1.000</td><td>0.800</td><td>0.4082</td><td>0.4085</td></th<>	~	, P	H	0.2500	0.3000	0.7000	0.7500	1.000	0.800	0.4082	0.4085
j0 I 0.2500 0.4500 0.7500 0.7700 0.7700 0.7700 0.7900 0.7900 0.2101 $j0$ I 0.2777 0.4266 0.6000 0.7790 1.000 0.399 0.1812 $j7$ I 0.2727 0.4266 0.6000 0.7790 1.000 0.399 0.1714 100 I 0.2727 0.4286 0.6000 0.7790 1.000 0.399 0.1714 200 I 0.2727 0.4286 0.6000 0.7590 1.000 0.399 0.1774 200 I 0.2727 0.4286 0.6000 0.7590 0.1793 0.1776 200 I 0.2727 0.4286 0.6000 0.7590 0.1776 0.1817 200 I 0.2727 0.42445 0.5730 0.1200 0.1776 200 I 0.2727 0.42466 0.5000 0.7790) 4	05	I	0.2500	0.3500	0.6500	0.7500	I.000	0.600	0.3073	0.3084
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jo jo jo o.2727 o.4286 o.6000 o.7500 I.000 o.359 o.5503 * $N =$ Number of plates.	22	05	iد.	0.2727	0.4286	0.6000	0.7500	I.000	0.359	0.3255	0.3574
N	23	30	50 20	0.2727	0.4286	0.6000	0.7500	I.000	0.359	0.5503	0.6601
	-	N =	mber of pla	tes.							

each wing. Such four-peak chromatograms are produced in each case where the four salts possess different K_D values. Fig. IC bears a close resemblance to the thin-layer chromatograms previously observed².

Table I reveals that the intensity distribution between outer and inner peaks, measured conveniently by $X^{12} + X^{21} = [\Sigma(C^1A^2) + \Sigma(C^2A^1)]/2$, is a function of the set of K_D values of the four salts. In working out this dependence (and that on K^M) it was necessary for the sake of economy to work principally with 50-plate runs. Fig. 2A shows that complete resolution about the center of symmetry of the chromatogram is achieved at about 200 plates, and that $X^{12} + X^{21}$ does not become constant

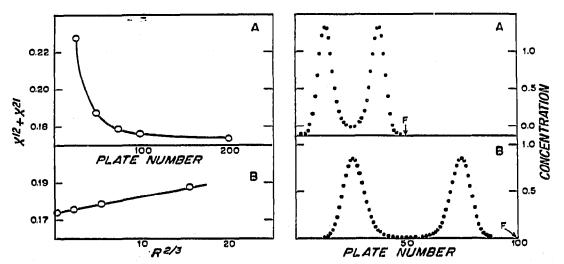


Fig. 2. Characteristics of the chromatograms of Fig. 1. $X^{12} + X^{21}$ (A) vs. number of plates; (B) vs. a function of the cross-hatched area of Fig. 4.

Fig. 3. Partition chromatogram of the system $CA_2^1 + CA_2^2 = CA^1A^2$, with $R_F^{11} = 0.25$, $R_F^{12} = 0.50$, $R_F^{22} = 0.75$ after (A) 50, (B) 100 plates.

until this point is reached. (Redistribution of material within the right and left halves of the chromatogram according to eqn. (I) can take place only through a region of overlap between the right and left halves.) Fig. 2 B uses a convenient extrapolation function to show that $X^{12} + X^{21}$ for the 200-plate chromatogram differs negligibly from that for complete resolution; the form of Fig. IC is thus quantitatively correct. The 50plate chromatograms were corrected approximately for the incomplete resolution by attributing the overlap area R (see Fig. 4A where the composition of a 50-plate peak is illustrated and R is shown as the cross hatched area) to the outer maxima, *i.e.* $(X^{12} + X^{21})$ cor. = 0.5 $\Sigma |(C^{1}A^{2})^{M} + (C^{1}A^{2})^{F} - (C^{2}A^{1})^{M} - (C^{2}A^{1})^{F}|$. This gave $X^{12} + X^{21}$ within about 3 % of the 200-plate value and this was considered acceptable. Material redistribution in the developing band substantially reduces the rate of resolution in these chromatograms in comparison with the separation of noninteracting substrates with the same R_F difference, as is shown in Fig. 4B.

 $X^{12} + X^{21}$ proves to be, to a close approximation, proportional to the quantity $(R_F^{21} - R_F^{12})/(R_F^{22} - R_F^{11})$ as illustrated in Fig. 5^{*}. There is a further minor de-

^{*} Here and elsewhere in this article the ions are so labelled that $R_F^{11} < R_F^{12} < R_F^{21} < R_F^{22}$; experimentally, of course, systems with $R_F^{21} < R_F^{12}$ are also observed², but the form of the chromatogram is not changed by this inversion.

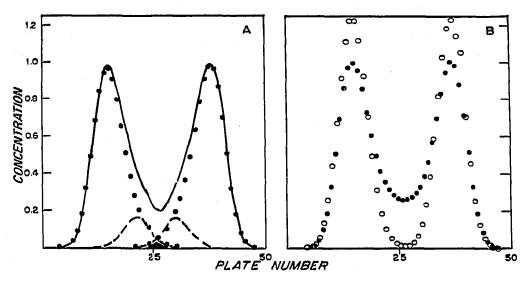


Fig. 4. Characteristics of chromatograms of the type of Fig. 1. (A) Breakdown of individual components for run 8 of Table I: \bigcirc , C¹A¹ and C²A²; ---, C¹A² and C²A¹; ----, total. (B) Comparison of run 18 (solid circles) with a chromatogram computed for two pure, noninteracting substances (open circles) having R_F values equal to those of C¹A¹ and C²A² in run 18. (Note that run 18 is the situation in which the reciprocal system eventually resolves into only two peaks).

pendence on the symmetry of the K_D^{ij} values about unity, with $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$ > I producing positive deviations in $X^{12} + X^{21}$ and vice versa. This is considered in a later section. In any case the principal intensity distribution is given by

$$X^{12} + X^{21} = 0.50 \ (R_F^{21} - R_F^{12}) / (R_F^{22} - R_F^{11}) \tag{10}$$

with an average deviation of 0.014 in $X^{12} + X^{21}$. Thus the chromatogram collapses to two spots only in the limit of $K_D^{12} = K_D^{21}$, and it approaches four spots of equal intensity only in the limit $K_D^{12} \longrightarrow K_D^{11}$, $K_D^{21} \longrightarrow K_D^{22}$. The point at $R_F^{11} \equiv R_F^{12}$, $R_F^{21} \equiv R_F^{22}$ is idiosyncratic, computation predicting (run 20) two peaks of pure C^1A^2 and C^2A^1 , *i.e.* $X^{12} + X^{21} = 1$ rather than 0.5 as predicted by eqn. (10). The value $X^{12} + X^{21} = 0$ at $R_F^{12} = R_F^{21}$ was difficult to demonstrate directly with precision. Since this point represents the minimum rate of resolution (Fig. 4B) a 100-plate run still shows an appreciable $X^{12} + X^{21}$ value (Table I). However, extra-

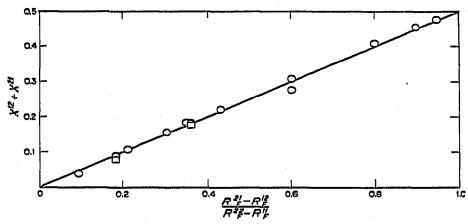


Fig. 5. Plot of $X^{12} + X^{21} vs. (R_F^{21} - R_F^{12})/(R_F^{22} - R_F^{11})$ according to eqn. (10).

(12)

(13)

polation of the 50- and 100-plate results, the general form of the $X^{12} + X^{21} vs$. $(R_F^{21} - R_F^{12})/(R_F^{22} - R_F^{11})$ dependence, and the analogy with the $CA_2^1 - CA_2^2 - CA_2^1 - CA_2^2$ system discussed in the next section together leave little doubt regarding this point.

The system $CA_2^1 - CA_2^2 - CA_1^2 A^2$

It is instructive to consider next the system of a bivalent cation with two monovalent anions for which eqn. (II) together with five equations analogous to (2)-(9)have been employed

$$CA^{1}_{2} + CA^{2}_{2} \rightleftharpoons 2 CA^{1}A^{2}$$
⁽¹¹⁾

in computations analogous to those of Table I. As Fig. 3 and Table II illustrate, this system does not give three spots, but only those due to CA_2^1 and CA_2^2 . Clearly this occurs, just as in the case of $C^1A^1-C^1A^2-C^2A^1-C^2A^2$ with $K_D^{12} = K_D^{21}$, because the two central ion pairs (2 CA^1A^2 or $C^1A^2 + C^2A^1$) remain physically superposed and are thus progressively converted via eqn. (1) or eqn. (11) to $CA_2^1 + CA_2^2$ or $C^1A^1 + C^2A^2$. With the rest of the systems of Table I on the other hand, C^1A^2 and C^2A^1 , having different R_F values, disengage physically before they are wholly consumed.

TABLE II

chromatograms of the system ${\rm CA^1}_2{\rm -CA^2}_2{\rm -CA^1A^2}$ computed according to distribution theory

N*	K^M	R_{F}^{11}	R_{F}^{12}	R_F^{22}	X ^{12 * *}
50	I	0.25	0.50	0.75	0.0176
100	I	0.25	0.50	0.75	0.0074

* N = number of plates.

** X^{12} = mole fraction of CA¹A².

The quotient $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$

If one writes the analog of eqn. (1) for the fixed phase

$$K^{F} = rac{(C^{1}A^{2})^{F} (C^{2}A^{1})^{F}}{(C^{1}A^{1})^{F} (C^{2}A^{2})^{F}}$$

it is clear that the partition equilibrium

is overdetermined and that

$$\frac{K^F}{K^M} = \frac{K_D^{12} K_D^{21}}{K_D^{11} K_D^{22}}$$

The situation $K_D^{12}K_D^{21}/K_D^{11}K_D^{22} = \mathbf{I}$ occupies a special position as the only case where K^F and K^M can both the unity, as would occur in the absence of ion association. This is the case corresponding to additivity of ionic contributions to the free energy of transport of $C^{i}A^{j}$ from one phase to the other³.

This is why eqn. (10) is strictly valid only for $K_D^{12}K_D^{21}/K_D^{11}K_D^{22} = K^F =$ $K^{M} = 1$, since otherwise, eqn. (1) and eqn. (12) will in general bias the material distribution of the chromatogram somewhat. If the residual error due to incomplete resolution is kept in mind, this bias is in the right direction to qualitatively account for the deviations in Fig. 5; quantitative corrections would be difficult to compute.

In most chromatographic systems ion association will be present, and $K_{D}^{12}K_{D}^{21}/K_{D}^{11}K_{D}^{22}$ values different from unity are expected. Data for thin-layer chromatography of quaternary ammonium iodides, bromides, nitrates and perchlorates² on silica gel G in chloroform-ethanol (24:1) provide 31 reciprocal salt systems for which the distribution of $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$ values is given in Table III.

TABLE III

DISTRIBUTION OF EXPERIMENTAL $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$ VALUES

Number of cases**
4
5
7
7
3
5

* Assigned such that $K_D^{11} > K_D^{12} > K_D^{21} > K_D^{22}$.

** Data from ref. 2.

It is of interest to attempt to account for the values of $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$ for these reasonably simple, near-spherical ions on the basis of simple electrostatic considerations. For a reciprocal ion pair equilibrium of the type

$$C^{\text{large}}A^{\text{large}} + C^{\text{small}}A^{\text{small}} \stackrel{K}{\leq} C^{\text{large}}A^{\text{small}} + C^{\text{small}}A^{\text{large}}$$
(14)

where the superscripts refer to the ionic radii, it is possible to demonstrate, assuming only that the distances of closest approach are sums of constant ionic contributions, that the electrostatic contribution to eqn. (14) is such as to favor ClargeAlarge + C^{small}A^{small}, *i.e.* make $K < 1^*$. Increase in the dielectric constant of the medium will then reduce in magnitude the electrostatic energies and make K approach unity, *i.e.* increase K. If one makes the reasonable assumption that the fixed phase in these thin-layer chromatograms is the more polar phase, this requires that

$$\frac{K^F}{K^M} = \frac{K_D^{12} K_D^{21}}{K_D^{11} K_D^{22}} > 1$$

* This problem reduces to the following relations among the distances of closest approach: a < b < c < d and a + d = b + c, from which it is readily shown that (1/a + 1/d) > (1/b + 1/c). Since the electrostatic energy of the ion pair is proportional to I/a etc., this is a sufficient condition for the above rule.

when $C^1A^1 = C^{large}A^{large}$, $C^1A^2 = C^{large}A^{small}$, $C^2A^1 = C^{small}A^{large}$ and $C^2A^2 =$ C^{small}A^{small}. Thus, if the ion pairs are labelled (as throughout this paper) with C¹A¹ and C²A² the slowest and fastest species, respectively, the following should hold

 $K_D^{12}K_D^{21}/K_D^{11}K_D^{22} > 1$

if the slowest- and fastest-migrating ion pairs are ClargeAlarge and CsmallAsmall and

 $K_{D}^{12}K_{D}^{21}/K_{D}^{11}K_{D}^{22} < 1$

if the slowest and fastest ion pairs are ClargeAsmall and CsmallAlarge.

The test of this proposition is shown in Table IV.

In 24 of 29 cases (83%) the prediction is correct. Furthermore, four of the five contrary cases involve systems where the two quaternary ammonium cations differ by only one CH₂ group in a 25-carbon atom ion, and the difference in R_F values is in fact not greater than their experimental uncertainties. The apparent success of this

TABLE IV

TEST OF THE ELECTROSTATIC MODEL FOR ESTIMATION OF $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$

<u></u>	Number of cases*	
	RF extremes are Clarge Alarge and CsmallAsmall**	R _F extremes are ClargeAsmall and CsmallAlarge**
K > 1	18	2
K < I	3	6

* Of the 31 systems, two had $K_D^{12}K_D^{21}/K_D^{11}K_D^{22} = 1.0.$ ** Ionic radii used (Å): I⁻, 2.16; ClO₄⁻, 2.00; Br⁻, 1.95 (GRUNWALD, BAUGHMAN AND KOHN-STAM⁴); NO₃⁻, 1.75-1.85 (PAULING⁵ and MESCHEL AND KLEPPA⁶).

simple model implies that the forces determining K^F and K^M are predominantly electrostatic and that the extrapolation of distribution phenomena to treat the thinlayer chromatograms (which are in large part adsorption chromatograms) is a usable one.

It is not surprising that (Tables III and IV) the cases of coincidence of ion pair radius sum-and chromatographic mobility-extremes outnumber the cases of noncoincidence nearly three fold (21:8). In every one of the coincident cases, moreover, Clarge Alarge is the fastest, C^{small}A^{small} the slowest species. Thus the fastest species are distributed among the types ClargeAlarge, ClargeAsmall, CsmallAlarge and CsmallAsmall in the ratio 21:8:0:0, reflecting the expected preference of the larger ions for the less polar phase⁷, as well as a predominance of the influence of the cation.

The magnitude of K^M

Table I (runs 8, 21–23) gives the variation in $X^{12} + X^{21}$ produced by variation of the input value of K^{M} . The generalizations of the preceding paragraph imply that the most common deviation from eqn. (10) will be that in which the extreme peaks are enriched at the expense of the inner peaks. Quite sizeable values of K^M can arise

from purely electrostatic contributions. For instance a system with ionic radii of 1, 1, 5 and 5 Å (perhaps the most extreme case involving relatively simple ions) in a medium of dielectric constant = 10 generates $K^{M} = 2 \cdot 10^{-7}$. On the other hand, the systems of Tables III and IV probably have $0.8 \leq K^M \leq 1.0$. It is interesting to note that values of K (eqn. 14) obtained by GRISWOLD, JONES AND BIRDWHISTELL⁸ from salt effects on salt solubilities in acetic acid can be accounted for rather well by the electrostatic model. For Li+-K+-Br--acetate- (or formate-) they report 0.136 (0.178) vs. 0.13 calculated taking the effective radius of RCO_2^- equal to that of hydroxide ion; similarly for Na+-K+-Br--acetate- (or formate-), 0.621 (0.556) vs. 0.42 calculated on the same basis.

With more complicated, perhaps polyfunctional ions, other forces can influence K^{M} , for example electron or proton donor-acceptor interaction. Representing acceptor and donor properties by the subscripts a and d, the system

$$C^{1}_{a}A^{1}_{d} + C^{2}_{d}A^{2}_{a} \stackrel{K^{M}}{=} C^{1}_{a}A^{2}_{a} + C^{2}_{d}A^{1}_{d}$$

could clearly have $K^M \simeq 10^{-4}$ from this source alone.

SUMMARY

A theoretical plate treatment of the partition chromatography of a reciprocal salt system has been carried out with the aid of a high-speed digital computer, and the results have been compared with the available experimental information. The following points were established.

1. The system of univalent cations C^1 and C^2 and univalent anions A^1 and A^2 produces, in general, four bands whose relative magnitudes are a function of the R_F values of the four possible ion pairs. The distribution of material when $K_D^{12}K_D^{21}/$ $K_D^{11}K_D^{22} = 1$ is given to a good approximation by

 $X^{12} = X^{21} = 0.25 \ (R_F^{21} - R_F^{12}) / (R_F^{22} - R_F^{11})$

where X^{11} , R_F^{11} and K_D^{11} are the mole fraction, R_F value and partition coefficient of the slowest species C^1A^1 etc.

2. The 2: I electrolyte system $C^{++}(A^1)^{-}(A^2)^{-}$ produces no band corresponding to CA¹A².

3. For simple ions in media in which the only important species are ion pairs, the magnitudes of the equilibrium constant K for $C^{1}A^{1} + C^{2}A^{2} = C^{1}A^{2} + C^{2}A^{1}$ can be estimated reliably from simple electrostatic considerations. The ratio of K values for the fixed and mobile phases of a partition chromatogram gives the important quotient $K_D^{12}K_D^{21}/K_D^{11}K_D^{22}$ whose deviation from unity can be qualitatively predicted from a knowledge of the ionic radii and the relative polarity of the two phases.

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